

Appendix F

Selected Solutions

F.2 Chapter 2 Solutions

2.1 The answer is 2^n

2.3 (a) For 400 students, we need at least 9 bits.

(b) $2^9 = 512$, so 112 more students could enter.

2.5 If each number is represented with 5 bits,

$$\begin{aligned} 7 &= 00111 \text{ in all three systems} \\ -7 &= 11000 \text{ (1's complement)} \\ &= 10111 \text{ (signed magnitude)} \\ &= 11001 \text{ (2's complement)} \end{aligned}$$

2.7 Refer the following table:

0000	0
0001	1
0010	2
0011	3
0100	4
0101	5
0110	6
0111	7
1000	-8
1001	-7
1010	-6
1011	-5
1100	-4
1101	-3
1110	-2
1111	-1

- 2.9 Avogadro's number (6.02×10^{23}) requires 80 bits to be represented in two's complement binary representation.
- 2.11 (a) 01100110
(b) 01000000
(c) 00100001
(d) 10000000
(e) 01111111
- 2.13 (a) 11111010
(b) 00011001
(c) 11111000
(d) 00000001
- 2.15 Dividing the number by two.
- 2.17 (a) 1100 (binary) or -4 (decimal)
(b) 01010100 (binary) or 84 (decimal)
(c) 0011 (binary) or 3 (decimal)
(d) 11 (binary) or -1 (decimal)
- 2.19 11100101, 111111111100101, 1111111111111111111111111100101. Sign extension does not affect the value represented.
- 2.21 Overflow has occurred if both operands are positive and the result is negative, or if both operands are negative and the result is positive.
- 2.23 Overflow has occurred in an unsigned addition when you get a carry out of the leftmost bits.

- 2.25 Because their sum will be a number which if positive, will have a lower magnitude (less positive) than the original positive number (because a negative number is being added to it), and vice versa.
- 2.27 The problem here is that overflow has occurred as adding 2 positive numbers has resulted in a negative number.
- 2.29 Refer to the following table:

X	Y	X AND Y
0	0	0
0	1	0
1	0	0
1	1	1

- 2.31 When atleast one of the inputs is 1.
- 2.33 (a) 11010111
 (b) 111
 (c) 11110100
 (d) 10111111
 (e) 1101
 (f) 1101
- 2.35 The masks are used to set bits (by ORing a 1) and to clear bits (by ANDing a 0).
- 2.37 $[(n \text{ AND } m \text{ AND } (\text{NOT } s)) \text{ OR } ((\text{NOT } n) \text{ AND } (\text{NOT } m) \text{ AND } s)] \text{ AND } 1000$
- 2.39 (a) 0 10000000 111000000000000000000000
 (b) 1 10000100 101110101110000000000000
 (c) 0 10000000 10010010000111111011011
 (d) 0 10001110 111101000000000000000000
- 2.41 (a) 127
 (b) -126
- 2.43 (a) Hello!
 (b) hELLO!
 (c) Computers!
 (d) LC-2
- 2.45 (a) xD1AF
 (b) x1F
 (c) x1

(d) xEDB2

2.47 (a) -16

(b) 2047

(c) 22

(d) -32768

2.49 (a) x2939

(b) x6E36

(c) x46F4

(d) xF1A8

(e) The results must be wrong. In (3), the sum of two negative numbers produced a positive result. In (4), the sum of two positive numbers produced a negative result. We call such additions OVERFLOW.

2.51 (a) x644B

(b) x4428E800

(c) x48656C6C6F

2.53 Refer to the table below:

A	B	Q1	Q2
0	0	1	0
0	1	1	1
1	0	1	1
1	1	0	1

Q2 = A OR B

2.55 (a) 63

(b) $4^n - 1$

(c) 310

(d) 222

(e) 11011.11

(f) 0100 0001 1101 1110 0000 0000 0000 0000

(g) 4^{4m}